

## Sound Insulation of Monolithic or Laminated Single- and Double-Glazing Panels

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### ABSTRACT

Sound transmission characteristics of single or multiple panels as sound insulation components in buildings have been studied extensively, and numerous models have been developed over the past few decades. Though most of them have been validated individually with specific test results in their developing phases, evidence showed that considerable discrepancy exists from one model to another. By applying many existing models onto glazing panels such as windows, doors, or building facades, the authors found that most of them unable to accurately predict their sound insulation performance. Apparent discrepancy up to 3-5 dB in terms of OITC/STC index was even found between the predictions by commercial software and those well-recognized test results. More accurate theoretical models are highly demanded in the industry to guide the design of real practice. To address this need, revisits of most existing theoretical models were made by the authors, and extended models are accordingly developed and presented in this study to provide more accurate predictions on the acoustic performance of monolithic or laminated single- and double-glazing panels. Test results collected from literature as well as conducted by the authors are further provided to validate the proposed models.

**Keywords:** Sound radiation, Insulation, Sound Transmission Loss, glazing panel, laminated glass

### 1. INTRODUCTION

The acoustic performance of building facades such as window, door, and curtain wall in terms of their sound insulation is one of the critical calibers to the quality of Schüco products across the world. Architecture designer, general engineer or contractor are heavily relying on commercial software to estimate the acoustic performance of certain designed products. However, majority of them do not necessarily have the knowledge sensing whether the estimations provided by the software reflecting the reality of the product or will meet the need from customers. In this sense, the accuracy of the theoretical models behind any commercial software plays a considerable role in designing a product.

Over the past few decades, numerous models have been developed to predict the sound transmission characteristics of single or multiple layer panels. In many theoretical models, various constants or parameters were empirically determined by best matching the predictions with test results. As a consequence, a model might work well for a certain type of materials while not applicable to others. Moreover, evidence showed that considerable discrepancy exists from one model to another. By applying many existing models onto single or multiple glass panels, the authors found that most of them unable to accurately predict their sound insulation performance. Apparent discrepancy up to 3-5 dB in terms of OITC/STC index was found between the predictions by commercial software and those well-recognized test results, which is even higher for multiple layer laminated glass panels.

In this study, based on existing theoretical models of sound transmission loss on single and multiple panels, extended models are developed and summarized for a single layer of laminated glass and a double layer of insulating-laminated glass panels. Test results collected from literature as well as

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conducted by the authors are further provided to validate the extended models.

## 2. SINGLE LAYER GLAZING PANEL

### 2.1 Monolithic Glazing

#### 2.1.1 Current models in the literature

From Davy's studies (1–3), the diffuse field sound transmission coefficient of a single rectangular homogeneous panel with dimensions of  $a \times b$  can be calculated as

$$\tau = \begin{cases} \tau_l = \frac{2}{\alpha_0^2} \left( \ln \left( \frac{1 + \sqrt{1 + q^2}}{p + \sqrt{p^2 + q^2}} \right) + \frac{1}{\lambda} \ln \left( \frac{h + \sqrt{h^2 + q^2}}{p + \sqrt{p^2 + q^2}} \right) \right), & f \leq f_c \\ \tau_h = \frac{\sigma_0^2}{2\alpha_0 r_f (\sigma_0 + \alpha_0 \eta)} \left( \arctan \left( \frac{2\alpha_0}{\sigma_0 + \alpha_0 \eta} \right) - \arctan \left( \frac{2\alpha_0(1 - r_f)}{\sigma_0 + \alpha_0 \eta} \right) \right), & f > f_c \end{cases} \quad (1)$$

where the radiance efficiency  $\sigma_0$  in high frequency ( $f > f_c$ ) is given by  $\sigma_0 =$

$$\begin{cases} \frac{1}{\sqrt{g^{n+q^n}}}, & \text{if } p \leq g \leq 1 \\ \frac{1}{\sqrt{(h-\lambda \cdot g)^{n+q^n}}}, & \text{if } 0 \leq g \leq p \end{cases} \quad \text{with parameters summarized as } \alpha_0 = \pi f \frac{m}{\rho_0 c}; r_f = \frac{f}{f_c}; p = \min \left( \zeta_1 \sqrt{\frac{\pi}{2k\alpha_0}}, 1 \right); q = \frac{2\pi}{k^2 A_s}; g = \begin{cases} 0, & \text{if } f \leq f_c \\ \sqrt{1 - f_c/f}, & \text{if } f \geq f_c \end{cases}; h = \frac{1}{\frac{2}{3} \sqrt{\frac{\pi}{2k\alpha_0}} - \zeta_2}; \lambda = h/p - 1, \text{ and } m \text{ is the}$$

surface density of the panel,  $\rho_0$  the ambient air density,  $c$  the sound speed traveling in the ambient air,  $\eta$  the total damping loss factor of the panel, wave number  $k = 2\pi f/c$ ,  $A_s$  the area of the panel,  $\alpha_0 = \frac{A_s}{a+b}$  the dimension of the panel by considering it as an equivalent square panel;  $n, \zeta_1$  and  $\zeta_2$  are empirical constants which are suggested to take the value of  $n = 2, \zeta_1 = 1.3$ , and  $\zeta_2 = 0.124$ .

The total damping loss factor is the sum of the internal damping loss factor  $\eta_0$  and that due to the transmission of vibrational energy from the panel to its surrounding elements  $\eta_e$ . According to Annex C of ISO 12354-1:2017(E)(4),  $\eta_e$  can be evaluated for structural elements with a surface mass  $m \leq 800 \text{ kg/m}^2$  as  $\eta_e = \frac{m}{485\sqrt{f}}$ . The critical frequency can be determined by  $f_c = \frac{c^2}{2\pi} \sqrt{\frac{M}{B}}$ , where  $B = \frac{Et^3}{12(1-\nu^2)}$  is the bending stiffness of the panel.

From the sound transmission coefficient determined in Eq. (1), the sound transmission loss (STL) of a single homogeneous panel can be calculated by  $\text{STL} = -10\lg(\tau)$ . To better match the prediction of STL with experimental results, it was proposed that the sound transmission coefficient below the critical frequency  $\tau'_l$  is calculated as the sum of  $\tau_l$  and  $\tau_h$  in Eq. (1) by accounting for the bending stiffness effect.

#### 2.1.2 Modifications

Though it was identified that Davy's model provides closest evaluations of STL for single glazing panels in the current literature (5), the authors found that near the resonant and critical frequencies, considerable discrepancies exist between the prediction of the STL by Davy's model and the test results, often there is about 2 - 3 dB discrepancy in terms of STC/OITC index. To address this issue, certain revisions were made by the authors (5) by adding two more sections within the lower frequency range and adjusting the radiation efficiency to improve the predictions based on Davy's models. Accordingly, the revised sound transmission coefficient of the panel is given by

$$\tau = \begin{cases} \tau_{l1} = \frac{1}{\alpha_0^2} \ln \left( \frac{1 + \alpha_0^2}{1 + \alpha_0^2 \cos b} \right), & f \leq 2f_l/3 \\ \tau_{l2}, & 2f_l/3 \leq f \leq f_l \\ \tau_m = \tau'_l, & f_l \leq f \leq f_c \\ \tau_h, & f > f_c \end{cases} \quad (2)$$

where  $f_l = \frac{\pi c_L t}{4\sqrt{3}} \left( \left(\frac{1}{a}\right)^2 + \left(\frac{1}{b}\right)^2 \right)$  is the resonance frequencies of the panel,  $c_L = \sqrt{\frac{E}{\rho(1-\nu^2)}}$  the propagation velocity of the quasi-longitudinal wave in the glazing panel;  $E, \rho, \nu$  are Young's modulus, density and Poisson ratio of the panel, respectively,  $\cos_b^2 \theta$  is an associate parameter to consider the practical limitation of sound radiation angle, which is given by (6) as  $\cos_b^2 \theta = \min\left(\frac{1}{k\sqrt{A_s}}, 0.9\right)$ ,  $\tau_{l2}$  is determined by linear interpolation of  $\tau_{l1}$  and  $\tau_m$ . To better match the predictions with test results, the original radiation efficiency  $\sigma_0$  of single glazing is replaced by  $\sigma_1 = \begin{cases} \sigma_0, & f \leq 0.9f_c \\ \min(\sigma_0, \sigma_c), & f \geq f_c \end{cases}$ , while between  $0.9f_c$  and  $f_c$ , it is obtained by linear interpolation, and  $\sigma_c$  is a critical radiation efficiency to filter out the unrealistic high value at critical frequency.

Figure 1 provides an overall comparison of the STL for a 1/2 inch monolithic glass panel (with dimension of 36 in by 84 in) among Viracon test result (7), simulation by INSUL 9.0 (8), original prediction by (1), and the modified model (5). In comparison with measurements in the third-octave band, the theoretical values were averaged over the three frequencies which were 2-1/9, 1, and 21/9 times the center frequency of the third-octave band if the critical frequency locates within the measurement frequency (so does in the rest of the STL charts in this paper). Nearby the resonance frequencies of the panel, it shows 3~4 dB difference of sound transmission loss between the original model and the modified one.

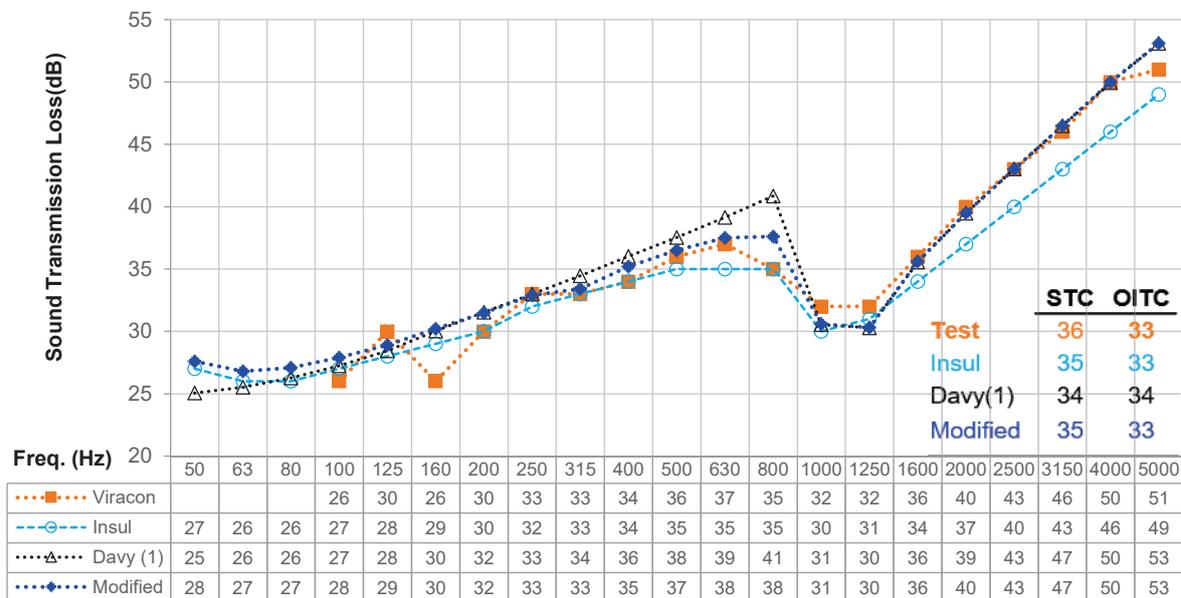


Figure 1 - STL of 1/2 inch monolithic glass panel (36 in by 84 in)

## 2.2 Laminated Glazing

Laminated glass has been gaining more applications in industry as it provides better performance for structural, acoustical, and thermal performances. Laminated glass is achieved by bonding two or more glass plies with thermoplastic polymeric interlayers. The resulting laminated glass performs much safer than monolithic glass because the fragments remain attached to the interlayer even after breakage. To apply the extended model for the monolithic glass given in the previous section to laminated glasses, a laminated panel is considered as an equivalent single panel. The acoustic performance of a single laminated glass depends not only on individual layers but also on the interlayer and its dynamic performance. From this point of view, in addition to the effective properties of the laminated panel, the material properties of the interlayer must be included in the predicting model.

The effective thickness of the laminated panel is determined by following the procedures in ASTM E1300(9).

$$h_{ef,w} = \sqrt[3]{h_1^3 + h_2^3 + 12\Gamma I_s} \quad (3)$$

where  $\Gamma$  is the shear transfer coefficient which is a measure of the transfer of shear stresses across the interlayer  $\frac{1}{1+\chi\frac{E I_s h_d}{G h_s^2 a^2}}$ , where  $I_s = h_1 h_{s2}^2 + h_2 h_{s1}^2$ ,  $h_{s1} = \frac{h_s h_1}{h_1 + h_2}$ ,  $h_{s2} = \frac{h_s h_2}{h_1 + h_2}$ ,  $h_s = 0.5(h_1 + h_2) + h_f$ ,  $h_f$  is the interlayer thickness (mm),  $E$  the Young's modulus of glass,  $a$  the smallest in-plan dimension of the laminated panel, and  $G$  the interlayer storage shear modulus,  $\chi$  is a coefficient governed by boundary and loading conditions of the composite. For a laminated glass under the very particular case of simply supported and uniformly distributed loading, a value of  $\chi = 9.6$  was proposed by Wölfel (10).

For a laminated glass with fixed thicknesses of individual layers, it can be found from Eq. (5) that the effective thickness of the equivalent single glass keeps reducing as the thickness of the interlayer increases, which makes sense from a structural point of view but does not when the sound transmission is concerned. To better reflect the physics mentioned above, the equivalent thickness given in Eq. (5) is accordingly revised as  $h_{ef,ac} = h_{ef,w} + h_f/3$

Because of the existence of the viscoelastic polymer layer, the radiance of sound transmitting through the laminated glass varies accordingly, which varies as the type of the interlayer varies. Generally, the radiance decreases as the thickness of the polymer interlayer increases, more specifically, its decaying rate is larger for softer interlayer compared with that of the stiffer one. To reflect these trends, the radiance in laminated glass is proposed by introducing a decay factor  $\psi$  for the different interlayer, which is  $\sigma'_c = \sigma_c - \psi t_f$ , where  $\psi$  is determined by correlating the predictions with series of test results on laminated glass panel of different interlayers.

Figure 2 provides a comparison of the STL of a 1/2 single laminated glass panel (consists of two quarter inches monolithic glass combined with a 0.045 inch PVB thin layer, and dimension of 36 in by 84 in) among Viracon test result (7), simulation by INSUL 9.0 (8), and the present model. The comparison shows that the result predicted by Insul general overestimates the STL, especially at a frequency higher than the critical one, leading to an overestimated STC/OITC index. However, the present model can match the test result almost over the entire frequency range except those nearby the resonant one where a spike exhibit, which might result from collected error because of practical difficulties or uncontrollable boundary effects during a test at a lower frequency.

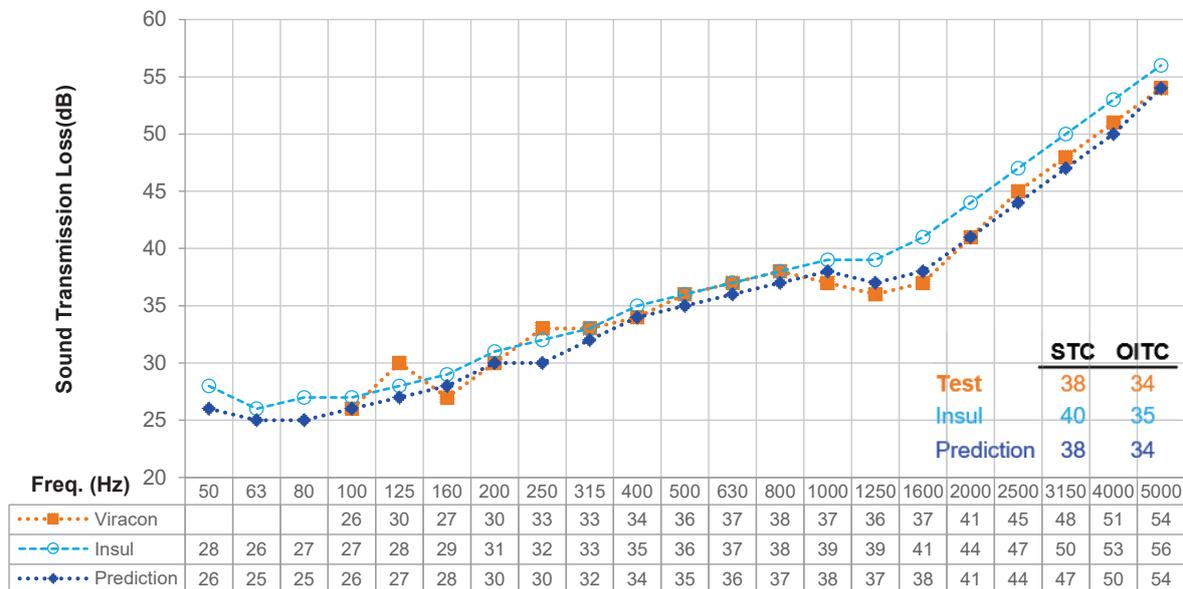


Figure 2 - STL of 1/2 inch single laminated glass panel (36 in by 84 in)

### 3. DOUBLE-LAYER GLAZING PANEL

#### 3.1 Double-layer Monolithic Insulating Glazing

From Davy's studies (2,6,11,12), the diffuse field sound transmission coefficient of a double rectangular homogeneous panel with dimensions of  $a \times b$  can be summarized as

$$\tau = \begin{cases} \tau_{l1} = \frac{1}{\alpha_d^2} \ln\left(\frac{1 + \alpha_d^2}{1 + \alpha_d^2 \cos_b^2 \theta}\right), & f \leq 2f_0/3 \\ \tau_{l2}, & 2f_0/3 \leq f \leq f_0 \\ \tau_m = \frac{1 - \cos_m^2 \theta}{(q + p \cos_m^2 \theta)(q + p)}, & f_0 \leq f \leq k_0 \min(f_{c1}, f_{c2}) \\ \tau_{mh}, & k_0 \min(f_{c1}, f_{c2}) \leq f \leq \max(f_{c1}, f_{c2}) \\ \tau_h = \frac{\pi(\sqrt{r_{f1}} + \sqrt{r_{f2}})\mu}{4\alpha_1^2 \alpha_2^2 \eta_1 \eta_2 \delta_d^2 (\mu^2 + v^2)}, & f > \max(f_{c1}, f_{c2}) \end{cases} \quad (4)$$

where  $\tau_{l2}$  and  $\tau_{mh}$  are obtained from linear interpolations from their corresponding regions;  $\alpha_d = \alpha_1 + \alpha_2$  with  $\alpha_i = \pi f \frac{m_i}{\rho_0 c}$  and  $m_i$  is the surface density of the panel  $i$ , respectively; double panel resonant frequency (also known as the mass-air-mass frequency)  $f_0 = \frac{c}{2\pi} \sqrt{\frac{\rho_0}{d} \left(\frac{1}{m_1 + m_2}\right)}$  with  $d$  of the cavity gap between two panels;  $q = \frac{1}{2} \left(\frac{\xi_1}{\xi_2} + \frac{\xi_2}{\xi_1}\right)$ ,  $\xi_i = \alpha_i (1 - r_{fi}^2)$ ,  $p = \xi_1 \xi_2 \delta_d$ ,  $k_0 = 0.8$  is a constant, sound absorption coefficient of the wall cavity of the double leaf wall  $\delta_d = \delta_d(t_i, d)$  is determined by best matching a series of predictions and Viracon test results,  $\cos_m^2 \theta = \min\left(0.9, \max\left(\frac{1}{k\sqrt{A_s}}, 0.24\right)\right)$ ;  $r_{fi} = \frac{f}{f_{ci}}$ ,  $\mu = \eta_1 \sqrt{r_{f1}} + \eta_2 \sqrt{r_{f2}}$ , and  $v = 4(\sqrt{r_{f1}} - \sqrt{r_{f2}})$ .

To account for the stud born transmission effect between the two panels, the STL has been accordingly revised as

$$\tau = \begin{cases} \tau_{L1} = \tau_{l1}, & f \leq 2f_0/3 \\ \tau_{L2} = \tau_{l2}, & 2f_0/3 \leq f \leq f_0 \\ \tau_M = \tau_m + \tau_H + \tau_{SD}, & f_0 \leq f \leq k_0 \min(f_{c1}, f_{c2}) \\ \tau_{MH} + \tau_{SD}, & k_0 \min(f_{c1}, f_{c2}) \leq f \leq \max(f_{c1}, f_{c2}) \\ \tau_H = \frac{\int_0^1 \frac{dx}{(q_1^2 + (x - p_1)^2)(q_2^2 + (x - p_2)^2)}}{S_1^2 S_2^2 \delta_d^2} + \tau_{SD}, & f > \max(f_{c1}, f_{c2}) \end{cases} \quad (5)$$

where the stud born transmission efficiency  $\tau_{SD} = \frac{32\rho_0^2 c^3 D J_2}{G^2 b_0 (2\pi f)^2}$  with stud transmission ratio  $J_2 = \min\left(2/\left(1 + \left(1 - \frac{4\omega^{3/2} m_1 m_2 c C_M}{G}\right)^2\right), K\right)$ ,  $C_M$  stud mechanical compliance, and  $K$  the minimum stud transmission; the space between studs is approximated as one third of the panel width, i.e.,  $b_0 = b/3$ ,  $G = m_1 \sqrt{2\pi f_{c1}} + m_2 \sqrt{2\pi f_{c2}}$ ,  $\tau_{MH}$  is determined by linear interpolations from  $\tau_M$  and  $\tau_H$  without considering  $\tau_{SD}$ ;  $p_i = 1 - \frac{1}{r_{fi}}$ ,  $q_i = \frac{1 + \frac{\alpha_i \eta_i}{\sigma_i}}{S_i}$ ,  $S_i = \frac{2\alpha_i r_{fi}}{\sigma_i}$ ,  $\sigma_i = \begin{cases} \sigma \sigma_i & f \leq 0.9 f_c \\ \min(\sigma_c, \sigma \sigma_i) & f \geq f_c \end{cases}$ ;  $\sigma \sigma_i = \begin{cases} \frac{1}{\sqrt{g_i^{n+q^n}}}, & \text{if } p \leq g_i \leq 1 \\ \frac{1}{\sqrt{(h-\lambda \cdot g_i)^{n+q^n}}}, & \text{if } 0 \leq g_i \leq p \end{cases}$  and critical radiation efficiency  $\sigma_c$  is determined by the gap of the cavity between the two panels and their relative thickness as  $\sigma_c = \sigma_c(t_i, d)$ . Note that many inconsistencies exist in determining the parameters values in Eqs. (4) and (5) among Davy's studies on double panels (2,6,11,12), some of them have been accordingly reunified and modified in this study such that best agreement is achieved between the predictions and test results.

### 3.2 Double-layer Laminated Insulating Glazing

The STL of insulating-laminated (one layer monolithic and the other layer laminated) and double laminated insulating (both layers are laminated) are developed based on section 3.1. In this model, the laminated layers are firstly treated as an equivalent single layer by following the approach in section 2.2, sound absorption coefficient and critical radiation efficiency are then determined by regression analysis and reconstructed as a function of the thickness of individual layers and the cavity gap between them as  $\delta'_r(t_i, t_f, d)$  and  $\sigma'_c(t_i, t_f, d)$ , where  $t_i$  is the equivalent thicknesses of laminated layers ( $i = 1, 2$ ) and  $t_f$  the thickness of the interlayer.

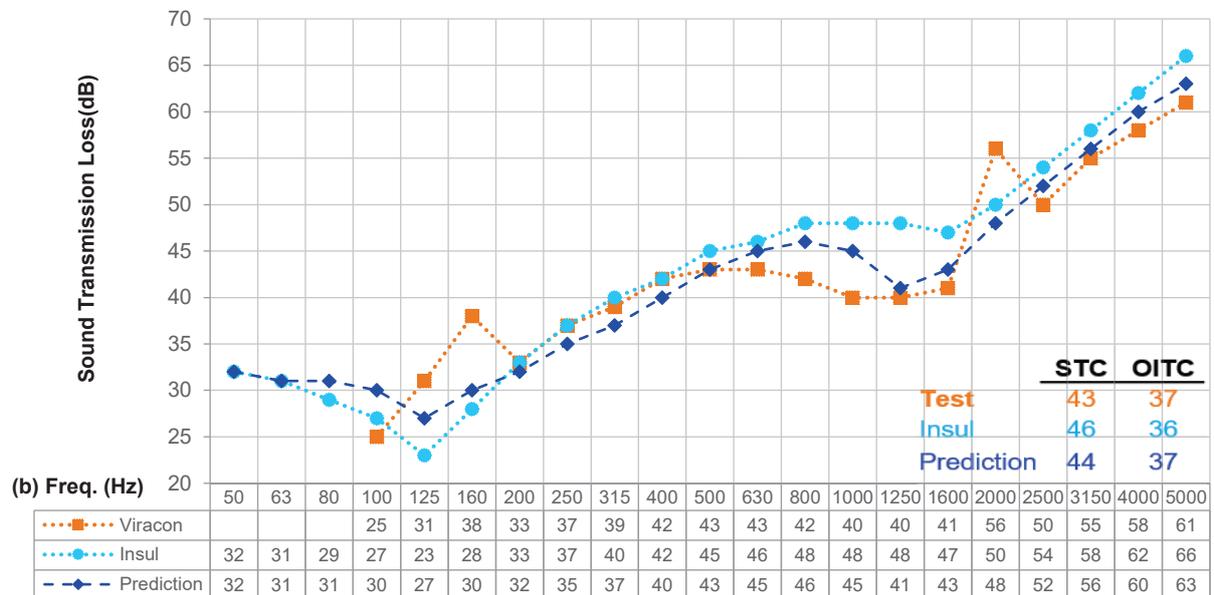
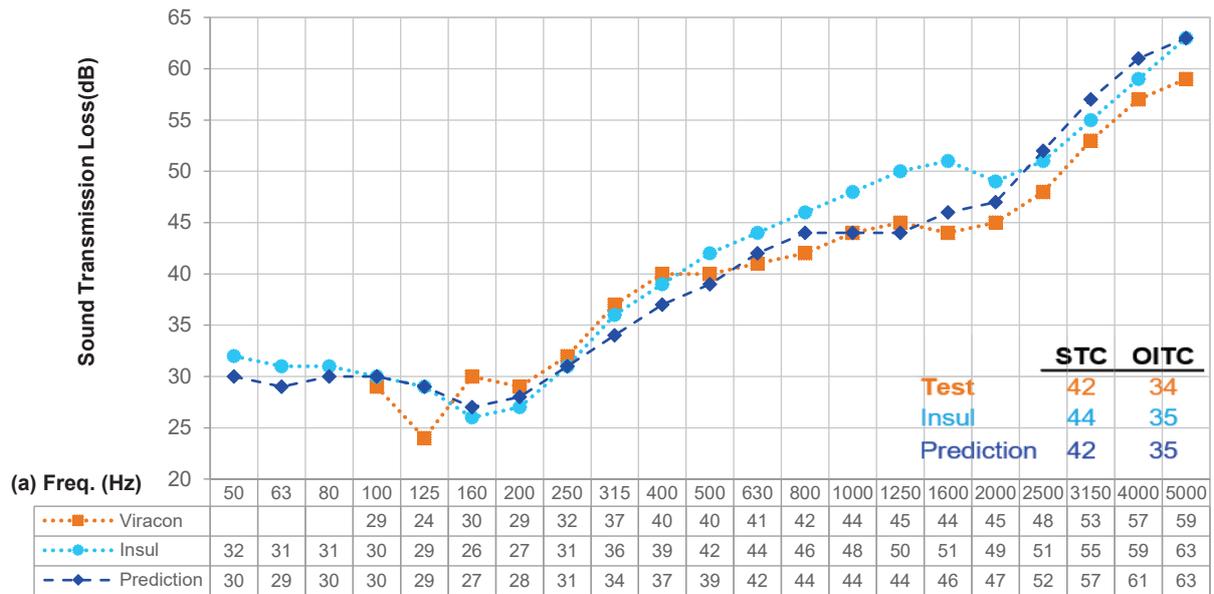


Figure 3 – STL of insulating-laminated double layer glass panel: (a) 1-3/16" overall - 1/4" glass, 1/2" airspace, 3/16" glass, 0.060" PVB, 3/16" glass; and (b) 1-11/16" overall - 3/8" glass, 3/4" airspace, 1/4" glass, 0.060" PVB, 1/4" glass

Comparisons of the STL for two different insulating-laminated double layer glass panels among Viracon test, Insul simulation results, and the present model are provided in Figure 3(a) and (b). The overall thickness of these two panels are 1-3/16" and 1-11/16", respectively. The results show that in general both the present model and Insul agree with the test results and they can provide similar dips at the double panel resonant frequency and coincident frequency. However, nearby the coincide frequency Insul predicts much higher STL than the test results while the present model well aligns with the test result.

Figure 4 shows the comparisons of the STL for two different double layer laminated glass panels among Viracon test, Insul simulation results, and the present model. At relatively low frequencies (below critical frequency of individual panels), the results predicted by Insul and the present model fairly agree with the test results. At higher frequency (above coincidence frequency), the present model still can reasonably match the test results. However, Insul significantly overestimates the STL, with a discrepancy up to 8 dB for the STC index. The theoretical model behind Insul is not able to provide a reliable prediction of STL for double layer laminated glass panels, especially when the overall thickness of the double laminated glass panel is large.

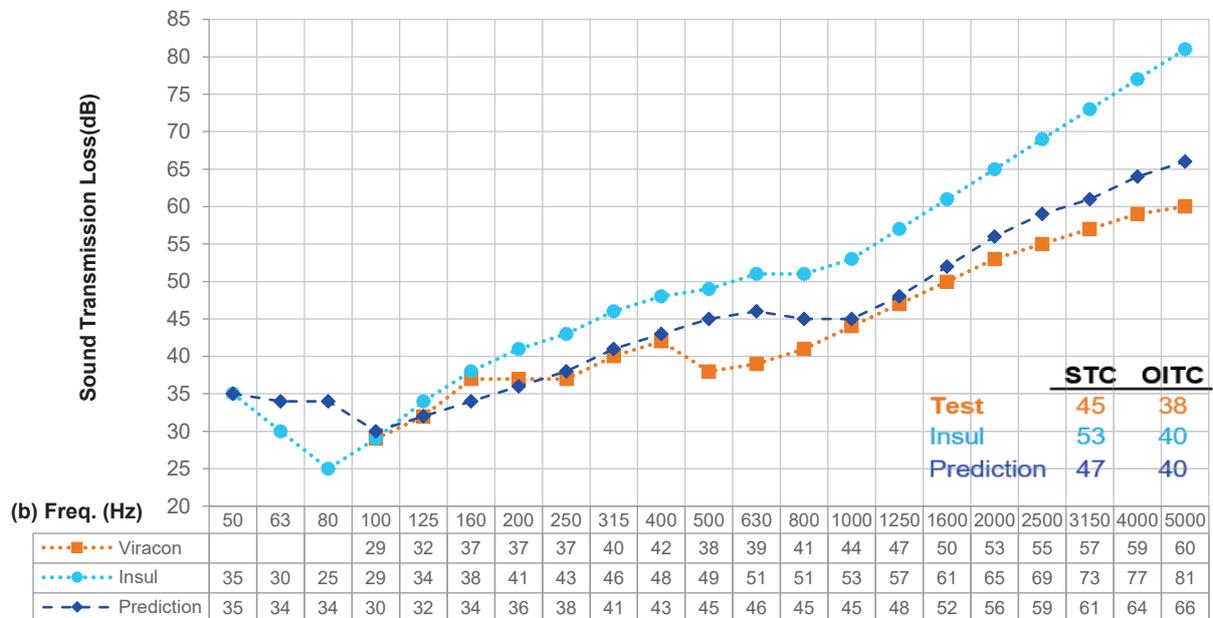
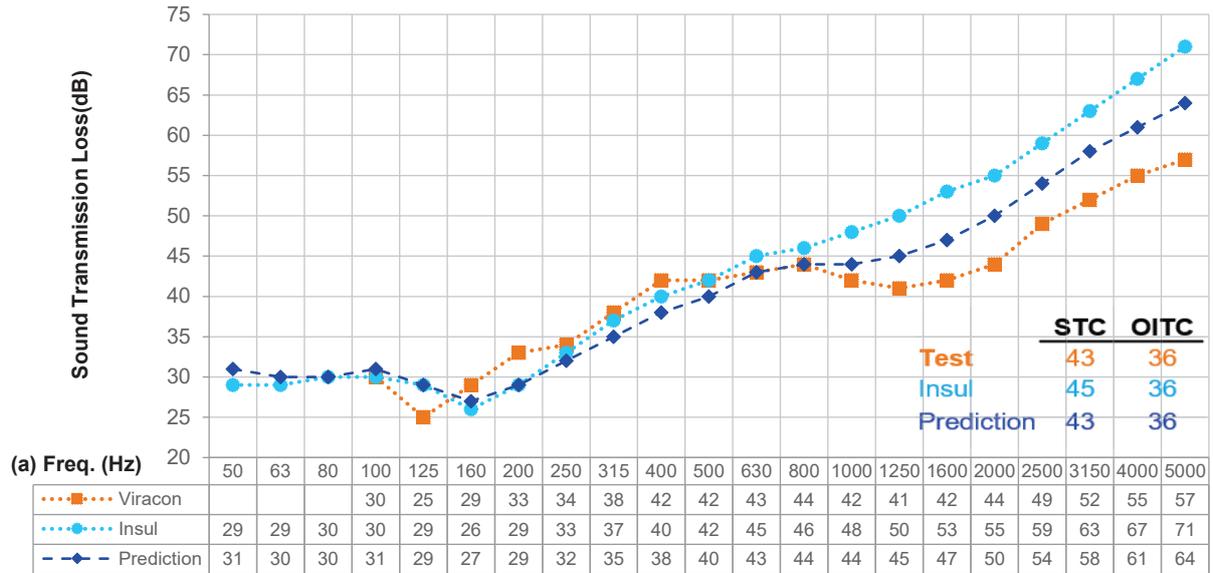


Figure 4 – STL of double-laminated double layer glass panel: (a) 1-5/16" overall - 1/4" glass, 0.030" PVB, 1/4" glass, 1/2" airspace, 5/32" glass, 0.060" PVB, 5/32" glass, 3/16" glass; and (b) 2-5/8" overall - 3/8" glass, 0.060" PVB, 3/8" glass, 1" airspace, 3/8" glass, 0.090" PVB, 3/8" glass

#### 4. CONCLUSIONS

Based on existing theoretical models of sound transmission loss on single and multiple panels, extended models have been developed for single and double insulating-laminated glass panels in this study. Various comparisons among test results and simulation predictions by Insul are provided to validate the extended models.

For single laminated glass panel, the comparison shows that the result predicted by Insul general overestimates the STL, especially at frequencies higher than the critical one, leading to an overestimated STC/OITC index. For double laminated glass panels, comparison results show that the predictions provided by Insul considerably overestimate the STL, with a discrepancy up to 8 dB in terms of the STC index for relatively thicker double laminated glass panel, indicating that the theoretical model behind Insul is not able to provide reliable prediction of STL for laminated glass panels. In other words, Insul usually considerably overestimates the STL for high performance double

laminated glass panels.

Well agreements among the predictions by the present models and test results for various single or double laminated glass panels, however, demonstrate the viability of the present models. It is worthy to note that the presented models were calibrated by comparing test results only from various glass panels. The applicability of the presented models to other building materials such as gypsum board, brick or masonry wall has not been investigated yet.

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