

[Open-source platforms for fast room acoustic simulations in complex structures]

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Abstract

This article presents new numerical simulation tools, respectively developed in the Matlab and Blender environments. Available in open-source under the GPL 3.0 license, it uses a ray-tracing/image-sources hybrid method to calculate the room acoustics for large meshes. Performances are optimized to solve problems of significant sizes (typically more than 100,000 surface elements and about a million of rays). For this purpose, a Divide and Conquer approach with a recursive binary tree structure has been implemented to reduce the quadratic complexity of the computation of ray/element interactions to near-linear. Thus, execution times are less sensitive to the mesh density, which allows simulations of complex geometries. After ray propagation, a hybrid method leads to image-sources, which can be visually analyzed to localize sound map. Finally, impulse responses are constructed from the image-sources and FIR filters are proposed natively over 8 octave bands, taking into account material absorption properties and propagation medium. This algorithm is validated by comparisons with theoretical test cases. Furthermore, an example on a quite complex case, namely the ancient theater of Orange is presented.

Keywords: Room acoustics, ray-tracing, fast methods, open-source

1 INTRODUCTION

Today, digital technologies allow research to explore previously inaccessible areas, as virtual reality for archaeology. In this domain, many works focus on the visual restitution, but acoustic studies can reinforce researches to improve the understanding of the ancient world. For example, during the Roman Empire, architects have designed buildings using acoustic rules [3]. In this study, we focus on the ancient theater of Orange which has a significant size (100m wide), a complex geometry (ornaments, bleachers, columns, arches, etc.) and which is open-air. In a previous work, a complete mesh was designed using *Blender* CAD software [12]. To be representative, this mesh, shown in the figure 1, possesses 436 000 elements (triangular faces) and is accurate with respect to the actual archeological knowledge [5]. As the mesh size makes difficult the use of precise methods (FEM, BEM, etc.), ray-tracing approximation was performed, in order to compute fastly the full-band room impulse response (50 to 15000Hz). Under this assumption, open-source platforms were developed following two steps. We first build a prototype using *Gypsilab*, an open source MATLAB library for fast prototyping [1]. This preliminary work was useful to construct and validate ideas and algorithms. It leads to the creation of a new toolbox, *openRay*, now appended to the master branch of *Gypsilab* and freely downloadable [14]. In a second step, all algorithms were retranscribed in C++ using *Qt Creator*, leading to an autonomous tool *Just4RIR*. A python interface was added, in order to use this library as a *Blender* plug'in [15]. At the end, this plug'in allows archeologists to only work on *Blender*, modifying easily meshes and materials, run acoustic simulation and visualize results.

After reminders on acoustical energy propagation represented by ray-tracing, this paper gives implementation details of the method that was used to obtain a fast computation for large meshes. At the end, application on a virtual model of the ancient theater of Orange is performed.

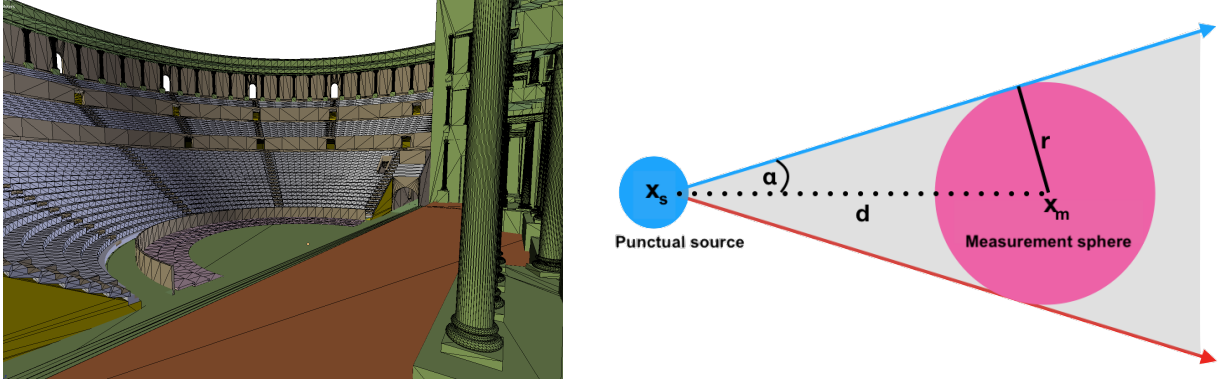


Figure 1. Left : Mesh of restituted theater of Orange modeled on *Blender* (436 000 triangles). Right : Representation of a r -radius measurement sphere centered in x_m , receiving energy from a sound source in x_s .

2 ACOUSTICAL ENERGY MODELIZATION

2.1 Continuous domain equation

Considering a sound source as a point source centered in \mathbb{R}^3 [6] and neglecting the losses due to the propagation medium, the normalized acoustical energy E is given by:

$$E = \int_{S_d} \mathbf{I} \cdot \mathbf{ds} = 1, \quad (1)$$

where S_d is a centered d -radius sphere and \mathbf{I} the acoustical intensity, such as:

$$\mathbf{I} = \frac{\mathbf{d}}{4\pi d^3}. \quad (2)$$

The energy obtained by integration on a portion σ_d of S_d satisfies:

$$E_\sigma = \int_{\sigma_d} \frac{\mathbf{d} \cdot \mathbf{n}}{4\pi d^3} ds = \frac{\Omega}{4\pi} \quad (3)$$

where Ω define a solid angle, characterizing a flow through the oriented surfaces σ_d . Thus, E_σ is constant for all radius d and corresponds to a portion of the total energy E . Finally, subdividing S in N portions σ_i , E can be decomposed as a sum of elementary energies:

$$E = \sum_{i=1}^N E_{\sigma_i} = \frac{1}{4\pi} \sum_{i=1}^N \left(\int_{\sigma_i} \frac{\mathbf{d} \cdot \mathbf{n}}{d^3} ds \right) = \frac{1}{4\pi} \sum_{i=1}^N \Omega_i. \quad (4)$$

2.2 Discrete model

To numerically represent the energy propagation of an omnidirectional sound source located in \mathbf{x}_s , we have to build a solid angle basis $(\Omega_i)_{i \in [1, N]}$ in equation (4). For this purpose, we introduce rays objects with:

- Source coordinates \mathbf{x}_i , with $\mathbf{x}_i = \mathbf{x}_s \ \forall i \in [1, N]$,
- Unitary direction \mathbf{u}_i , with an uniform sampling on the unitary sphere (e.g. [8]),
- Energy carried E_i , with $E_i = \frac{4\pi}{N} \ \forall i \in [1, N]$.¹

¹For directional sources, energies can be function of the direction.

As the acoustic source is discretized, we have to define a discrete measure of energy propagation. To this end, we consider a r -radius measurement sphere $S(x_m, r)$, centered on x_m (fig. 1). We can then add the contributions of a n -ray beam that intersects this sphere to calculate the acoustic energy E_m at the point x_m . In the particular case of an omnidirectionnal source, we have:

$$E_m \approx \frac{1}{4\pi} \sum_{i=1}^n \Omega_i \approx \frac{n}{N}, \quad (5)$$

which means that the measured energy E_m is statistically and naturally represented by the ratio between the number of rays forming a beam to the total number of rays. Furthermore, considering Ω_m the solid angle of the measurement sphere in figure 1:

$$\Omega_m = 2\pi(1 - \cos \alpha) = 2\pi \left(1 - \sqrt{1 - \frac{r^2}{d^2}} \right), \quad (6)$$

we observe for $r \ll d$ that:

$$\Omega_m \approx \pi \frac{r^2}{d^2} \Rightarrow E_m \approx \frac{n}{N} \approx \frac{\pi r^2}{4\pi d^2}. \quad (7)$$

For far measurements, approximation (7) expresses that E_m is well approximated by the ratio of the areas of the r -radius disk to the d -radius sphere. Otherwise, to ensure the existence of this last approximation, beams formed by n rays has to be measurable and count at least one ray ($n \geq 1$). This assumption is crucial to ensure the validity of the concept. Thus, fixing a measurement radius r , approximation (7) gives a maximum range of the discrete model:

$$d \leq \frac{r}{2} \sqrt{\frac{N}{n}}. \quad (8)$$

In addition, figure 2 shows how this statistic modelization represent the distance between source and measures. The accuracy of the measurement depends strongly on the number of rays counted, then, the more n increases, the more accurate will be the measurement. Nevertheless, in practice, values for a short distance between the source and the measurement sphere represent direct sound and first reflections, whereas long distances describe the diffuse field. Under this assumption, we can consider this model acceptable for all beam such as $n \geq 1$.

2.3 Presence of an obstacle

For the case of acoustic propagation in the presence of an obstacle, we choose to consider only specular reflections (Snell-Descartes laws). Indeed, this approximation is suitable when surfaces are larges in comparison to wavelengths and diffraction effects can be neglected [6]. For a room, this condition is reached if:

$$ka \gg 1, \quad (9)$$

with k the wave number and a the characteristic diameter of the room [9]. This approach is currently used by room acoustic softwares (e.g. *Odeon* [16], *Grasshopper* [13], etc.) regarding to audible frequency range (62,5 to 15000Hz). In particular, for the case of the theater of Orange considered in this paper which has a characteristic diameter of about 50 meters, fixing sound celerity to 340 m/s, the high frequency approximation is valid for $f \gg 1$ Hz.

When an incident ray intersects a flat surface, a reflected ray is generated from the collision point. Noting \mathbf{u}_i the direction vector of the incident ray, the reflected direction vector \mathbf{u}_r is defined by:

$$\mathbf{u}_r = (\mathbf{u}_i \cdot \mathbf{T})\mathbf{T} - (\mathbf{u}_i \cdot \mathbf{n})\mathbf{n}, \quad (10)$$

with \mathbf{T} the tangent basis and \mathbf{n} the normal vector to the surface. Moreover, we modify the energy of the reflected ray by:

$$E_r(f) = E_i(f)(1 - \alpha(f)), \quad (11)$$

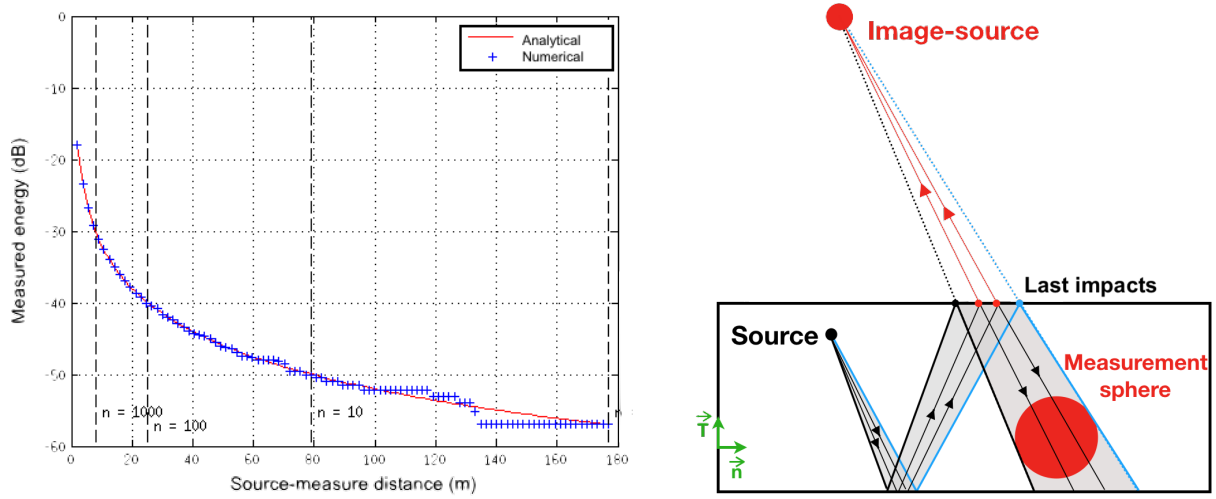


Figure 2. Left : Measured energy (dB) in function of distance between x_s and x_m , for $r = 0.36$ meter and $N = 10^6$ rays. Blue crosses stand for the statistical measure $f(r) = \frac{n(r)}{N}$ and red line the analytic function $f(r) = \frac{\pi r^2}{4\pi d^2}$. Right : Sketch of the creation of an image-source by successive reflections of rays on the walls of a room.

with $\alpha(f)$ the absorption coefficient of the surface that depends on of the frequency f . In practice, the absorption coefficients are often given per octave bands and can be found in various databases. Both *Gypsilab* and *Just4RIR* use the open access *Odeon* database [16] defined on eight octave bands.

Finally, considering wall absorption, energy measured statistically (eq. 7) is extended by:

$$E_m(f) \approx \frac{n}{N}(1 - \alpha(f)), \quad (12)$$

that we generalize to the case of m reflexions:

$$E_m(f) \approx \frac{n}{N} \prod_{j=1}^m (1 - \alpha_j(f)). \quad (13)$$

2.4 Image-sources

Although the generalized formulation (13) may be sufficient to generate room acoustic data, we also construct images-sources from the path of rays. To this end, when rays intersect the measurement sphere and following the reverse return principle, they are retro-propagated along the last direction vector. Thus, rays focus on punctual images-sources (fig. 2). Each image-source is then located relatively to the listener and carries an energy according to formulation (13).

By noting $(x_s)_{s \in [1, N_s]}$ the relative position of the N_s image-sources and $(E_s)_{s \in [1, N_s]}$ the associated energy, couples $(x_s; E_s(f))_{s \in [1, N_s]}$ contain all useful informations for room acoustic analysis and auralization. First of all, relative distance of each image-source $(d_s)_{s \in [1, N_s]}$ can be computed. These distances are also used to take into account the air absorption, by modifying equation (13) into:

$$E_s(f) \approx \frac{n}{N} e^{-\beta(f)d_s} \prod_{j=1}^m (1 - \alpha_j(f)), \quad (14)$$

with $\beta(f)$ a frequency dependent absorbing coefficient [11]. Furthermore, fixing the sound celerity c , room impulse response can be generated, converting each distance d_s in time of arrival. Paying attention to the

fact that the energy is proportional to the square of the pressure, the finite impulse response can be generated and analyzed using standard metrics (e.g. T_{30} , C_{80} , D_{50} , etc.). For auralization, this room impulse response is convolved with an audio signal in order to listen the acoustical rendering. In particular, this convolution can involve relative position of predominant images sources, in order to realize a spatialized auralization with multichannel or binaural renderers. Finally, to complete acoustic studies with visual analysis, images sources can be projected on the room used for computation in order to see where are located listened reflections (see last impact on figure 2).

3 IMPLEMENTATION

3.1 Standard algorithm

As common principles are introduced, we focus now on the numerical implementation of an acoustic renderer by ray-tracing. Before any acoustic computation, a numerical room has to be modeled with surfaces and materials. In our case, we use the classical representation with a mesh composed of flat triangles.

Using a discrete source point to initialize rays, geometrical intersections are computed between rays (L) and mesh elements (P) using parametric equations:

$$(L) : a + \delta \mathbf{u}, \quad \delta \in \mathbb{R}, \quad (15)$$

$$(P) : b + \lambda \mathbf{v} + \mu \mathbf{w}, \quad \lambda, \mu \in \mathbb{R}. \quad (16)$$

Considering \mathbf{v} and \mathbf{w} driven by two edges of each triangle, the following conditions give pairs (rays;elements) with uniqueness:

- $(0 \leq \lambda \leq 1)$, $(0 \leq \mu \leq 1)$ and $(\lambda + \mu \leq 1)$ to ensure that the intersection is inside the triangle,
- $\delta > 0$ to respect the propagation direction,
- δ minimum not to go through the whole mesh.

Practically, to find these pairs, we can solve directly the underlying linear system or use the Moller-Trumbler algorithm [7]. For N rays and M triangular elements, this process has a quadratic numerical cost (proportional to NM), which is critical if both N and M are large (see section 3.2).

Then, once all pairs are found, discrete measure has to be done in order to build images-sources (see section 2.4). To this end, the rays are intersected to the measurement sphere $S(x_m, r)$, which leads to a linear numerical cost proportional to N .

Finally, a ray is reflected according to equation (10) and propagated while its travelled distance verify condition (8). This iterative strategy ensure the energy propagation by the elimination of all rays that would be in non measurable beams. In the particular case of an open-air room, rays which don't intersect any surface of the mesh are also eliminated. Once all rays are eliminated, images-sources can be built and post-treated (room impulse response, auralization, etc.).

3.2 Tree-base acceleration

As we have seen, the most critical stage of the standard algorithm is the research of intersections between rays and triangular elements, leading a priori to a quadratic complexity $O(NM)$. Indeed, each ray has to be tested with each face, for each iteration of the ray-tracing algorithm. For a large number of mesh elements and rays which are needed to ensure reasonable accuracy (e.g. $M > 10^5$ and $N > 10^6$ for the Orange theater), the calculation time may be prohibitive. To solve this problem, a "Divide and Conquer" approach using a binary tree is performed.

The general principle consists in creating a mother-box, containing all the mesh elements. This mother-box is then subdivided along the largest dimension to create two daughter-boxes, each one possessing the same number

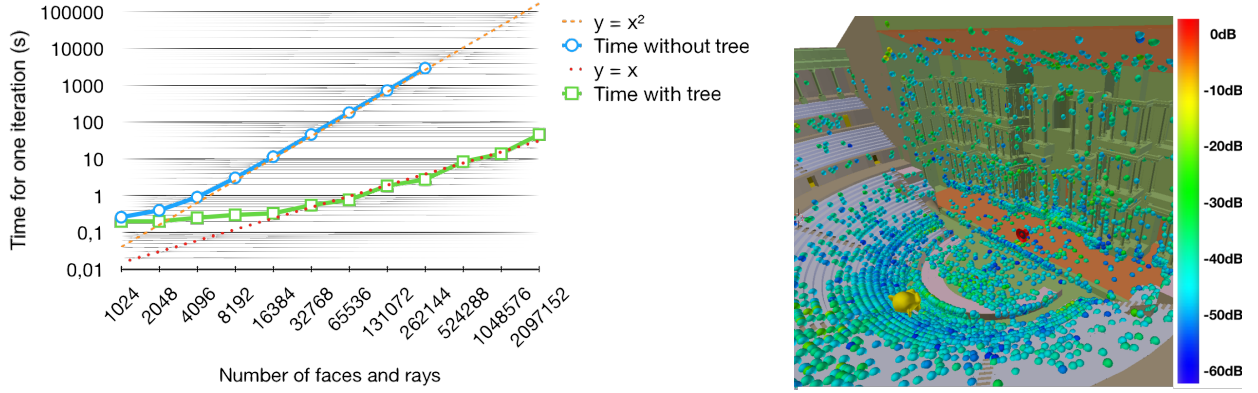


Figure 3. Left : Computation time for one iteration of ray-tracing in function of the number of face and rays, such as $N = M$ (log scale). An omnidirectional source is located at the center of a mesh of a unitary tetrahedral. Right : All images-sources projected on the mesh (up to RT60).

of elements (median spatial subdivision). This process is then applied recursively, until a stopping criterion is reached. In our case, we stop when the leaves contain only one element. This hierarchical tree is completely mesh dependent, computed in $O(M \log M)$ operations, and gives a structure which permits to quickly navigate inside the mesh.

Then, we initialize the ray sorting process starting from the mother-box, containing all rays and elements. Using the first tree-subdivision, we distribute rays inside the two daughter-boxes. This stage is done in $O(N)$ operations by the algorithm proposed by W. Amy *et al.* [10]. Indeed, each box has N_1 and N_2 rays, such as $N = N_1 + N_2$. Assuming this subdivision is performed recursively to the level p , the i^{th} box contains (N_i) rays with:

$$N = \sum_{i=1}^{2^p} N_i. \quad (17)$$

Then, ray sorting at the $(p+1)$ -level also conducts to $O(N)$ operations. To reach the level of the leaves, we have to perform $O(N \log M)$ operations, where $\log M$ is close to the depth of the binary tree. At the end, as we have only one element per box, the ray-element intersection only needs $O(N)$ operations. Finally, instead of $O(NM)$ operations, we compute all the intersections in:

$$O(M \log M) + O(N \log M) + O(N), \quad (18)$$

which operations is a near-linear complexity. Moreover, if the binary tree is precomputed, each iteration of the ray-tracing algorithm becomes:

$$O(N \log M) + O(N). \quad (19)$$

To evaluate numerically complexities with or without binary tree acceleration, we measure the computation time of one iteration by increasing the number of rays and the number of faces in the mesh ($N = M$). As we can see in figure 3, the complexity of the algorithm is therefore quasi linear by using tree-based method. This allows to treat large meshes with millions of rays, by keeping a reasonable computation time on a standard laptop (single core at 2.7 GHz and 8 Go ram).

4 APPLICATION TO ORANGE THEATER

In this paper, we focus only on the Orange Theater acoustics by ray-tracing. However, to evaluate and validate methods and algorithms, several non-regression tests have been detailed in R. Gueguen's PhD manuscript [5], associated to open-source implementation on *Gypsilab* [14] and *just4rir* [15] websites.

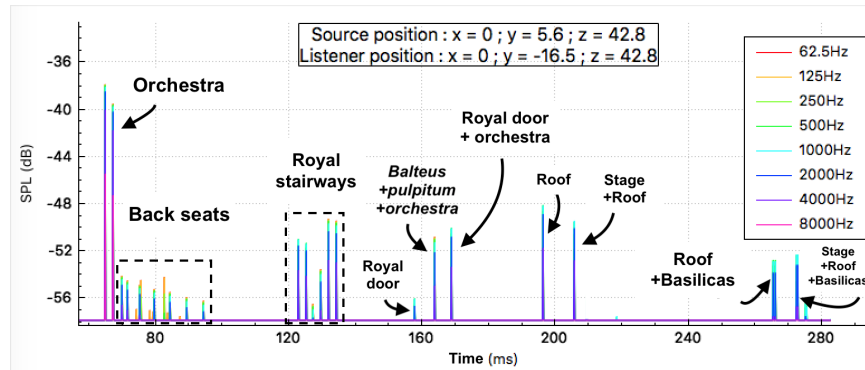


Figure 4. Impulse response in dB (early reflections, up to RT20).

First of all, a restituted version of the Orange theater has been realized on the software *Blender* (fig. 1), according to the archeological surveys performed by l'Institut de Recherche sur l'Architecture Antique [2]. As this mesh just needs to fill the geometry, there is no need of Delaunay properties, but the architecture complexity however leads to a triangulation with 436 000 faces. In particular, this virtual resitution is mainly composed by the *Post scaenium* (stage wall) partially ornamented with two basilicas on either side, the *Pulpitum* (stage), the *Orchestra*, the *Cavea* (bleachers) with *Porticus* at the top (column gallery) and various covers (stage roof, *velum*, etc.).

Several materials are assigned to each part of the theater, in order to define specific absorption coefficients taken from *Odeon* database [16]. The ray-tracing solver is then used to compute the spatial impulse response. To reach the reverberation time close to -60dB (RT_{60}), we fix one million rays and a 2m-radius measurement sphere. An omnidirectional source is located at the front stage, 1.60 m above the floor (this correspond to the position of the mouth of an average actor). The listener is on the same axis, in the bleachers.

The full ray-tracing propagation was done in few minutes on a standard laptop (2.7 GHz core and 8 Go ram). At the end, all sources-images projections are generated (fig. 3), illustrating a spatial diffusion of the sound source. Indeed, as some areas carry a lot of images-sources, reflections seem to surround the listener. More precisely, on figure 4, we see the early reflections of the multi-band echogramm of the theater (until RT_{20}). We can notice a high contribution of the *orchestra*, the wall-stage, the stage and the roof, as F. Canac demonstrated in the 60' [4].

To go further, many others results are available in R. Gueguen's PhD manuscript [5]. All results correspond to a room adapted for musical playback, more than a speech transmission. These results are confirmed by an equivalent simulation in the *Odeon* software (commercial license), using the same mesh and parameters.

5 CONCLUSION

In this paper, a full-chain engineering process is given, leading by an acoustical study of an imposing ancient monument. From archaeological needs, a fine mesh of the monument was constructed, associated to a complete room acoustic application suite, both for *MATLAB* and *Blender*. The high complexity provided by this type of architecture and its ornaments leads to approximate calculation methods. Indeed, by only simulating specular reflections and wall absorption, energy propagation and measurement can be simulated by beams, carried by ray-tracing. From this representation basis, it is possible to generate a multi-band impulse response, while respecting the laws of high-frequency acoustics. Moreover, a fast algorithm with a near-linear complexity has been implemented, allowing users to quickly evaluate architectural assumptions, modifying their meshes regardless of the number of elements. At the end, various post-treatments have been added, as the Room Impulse Response generation, the source-image visualization, the classical perceptive factors and an auralization process.

Even if current versions of proposed softwares (*Gypsilab* [14] and *Just4RIR* [15]) are complete enough to be used for various studies, there are many possibilities of improvement. First of all, as image-source positions are known, a spatial audio renderer could be added to improve current auralization tool (e.g. binaural or multi-channel, eventually with trackers). Secondly, as virtual reality is becoming more and more important in today's applications, we could consider moving the listener in real time and thus, allow a complete virtual tour of the building. Finally, as ray-tracing modelization is an high-frequency approximation of waves phenomena, diffraction effects should be added in order to get a better fit with the physical phenomena.

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