

# Performance Comparison of Single Channel Speech Enhancement Using Speech-Distortion Weighted Inter-Frame Wiener Filters

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## Introduction

Speech signals recorded in communication devices are frequently corrupted by undesired additive noise. To improve the speech quality, single-microphone noise reduction is often applied in the short-time Fourier transform (STFT) domain. In contrast to single-frame approaches, where a gain is applied to each noisy STFT coefficient independently, multi-frame approaches aim to exploit the speech inter-frame correlation (IFC) [1, 2, 3, 4].

In this paper, we investigate a real-valued speech-distortion weighted Wiener gain (SDW-WG) as well as real- and complex-valued speech-distortion weighted inter-frame Wiener filters (SDW-IFWFs) [1, 4]. These filters incorporate a trade-off between noise reduction and speech distortion. We compare these filters and analyze the influence of the corresponding trade-off parameter. Experimental results for different speech signals, noise types, and signal-to-noise ratios (SNRs) show that the real-valued SDW-IFWF (R-SDW-IFWF) achieves a higher speech quality improvement than the SDW-WG and complex-valued SDW-IFWF (C-SDW-IFWF). Although the SDW-WG applies more noise reduction than the multi-frame approaches, the C-SDW-IFWF introduces less speech distortion as the level of noise reduction is increased.

## Problem Statement

In this section, we introduce the single- and multi-frame signal models.

### Single-Frame Signal Model

By applying an STFT with analysis window  $h_F$  of length  $F$  to the noisy microphone signal, the noisy speech coefficient  $Y[f, l]$  with time frame  $l$  and frequency bin  $f \in \{-\frac{F}{2} + 1, -\frac{F}{2} + 2, \dots, \frac{F}{2}\}$  is obtained. The *single-frame signal model* is defined as

$$Y[f, l] = S[f, l] + N[f, l] \quad (1)$$

where  $S[f, l]$  and  $N[f, l]$  denote the speech and the noise coefficients, respectively. In single-frame approaches the speech coefficient  $S[f, l]$  is estimated by applying a (real-valued) gain  $G[f, l]$  independently to each noisy speech coefficient, i.e.,

$$\hat{S}[f, l] = G[f, l] Y[f, l] \quad (2)$$

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### Multi-Frame Signal Model

Similarly to (1), we apply an STFT to the noisy microphone signal with analysis window  $h_K$  of length  $K$ , to obtain the noisy speech coefficient  $Y[k, l]$  with frequency bin  $k \in \{-\frac{K}{2} + 1, -\frac{K}{2} + 2, \dots, \frac{K}{2}\}$ , which can be decomposed into the speech coefficient  $S[k, l]$  and the noise coefficient  $N[k, l]$ . The noisy speech vector  $\mathbf{y}[k, l]$  is defined by considering  $M$  consecutive time frames, i.e.,

$$\mathbf{y}[k, l] = [Y[k, l], Y[k, l-1], \dots, Y[k, l-M+1]]^T, \quad (3)$$

where  $T$  denotes the transpose operator. Similarly to (1), this vector can be written as

$$\mathbf{y}[k, l] = \mathbf{s}[k, l] + \mathbf{n}[k, l] \quad (4)$$

where the speech vector  $\mathbf{s}[k, l]$  and the noise vector  $\mathbf{n}[k, l]$  are defined similarly as in (3). In multi-frame approaches the speech coefficient  $S[k, l]$  is estimated by applying an  $M$ -dimensional (complex-valued) finite impulse response (FIR) filter  $\mathbf{w}[k, l]$  to the noisy speech vector, i.e.,

$$\hat{S}[k, l] = \mathbf{w}^H[k, l] \mathbf{y}[k, l] \quad (5)$$

where  $H$  denotes the Hermitian operator. For conciseness, in the remainder of this paper the indices  $f$ ,  $k$ , and  $l$  will be omitted wherever possible.

Assuming that the speech and noise signals are uncorrelated, the  $M \times M$ -dimensional noisy speech correlation matrix  $\mathbf{R}_y = \mathbb{E}[\mathbf{y}\mathbf{y}^H]$ , with  $\mathbb{E}[\cdot]$  the expectation operator, is given by

$$\mathbf{R}_y = \mathbf{R}_s + \mathbf{R}_n, \quad (6)$$

where  $\mathbf{R}_s = \mathbb{E}[\mathbf{s}\mathbf{s}^H]$  and  $\mathbf{R}_n = \mathbb{E}[\mathbf{n}\mathbf{n}^H]$  denote the speech and noise correlation matrices, respectively.

Considering the speech correlation across time frames, it was proposed in [1] to decompose the speech vector  $\mathbf{s}$  into a temporally correlated speech component  $\mathbf{x}$  and a temporally uncorrelated speech component  $\mathbf{x}'$  with respect to the speech coefficient  $S$ , i.e.,

$$\mathbf{s} = \mathbf{x} + \mathbf{x}' = \gamma_s S + \mathbf{x}', \quad (7)$$

where  $\gamma_s$  denotes the normalized speech IFC vector, which is defined as

$$\gamma_s = \frac{\mathbb{E}[\mathbf{s}S^*]}{\mathbb{E}[|S|^2]} = \frac{\mathbf{r}_s}{\phi_s}, \quad (8)$$

where  $*$  denotes the complex-conjugate operator and  $\mathbf{r}_s$  is the speech IFC vector. Due to the normalization with

the speech power spectral density (PSD)  $\phi_S = \mathbb{E}[|S|^2]$ , the first element of  $\boldsymbol{\gamma}_s$  is equal to 1.

Using (6) and (7), the speech correlation matrix  $\mathbf{R}_s$  can be decomposed into the rank-1 correlation matrix  $\mathbf{R}_x = \phi_S \boldsymbol{\gamma}_s \boldsymbol{\gamma}_s^H$  and the correlation matrix  $\mathbf{R}_{x'} = \mathbb{E}[\mathbf{x}' \mathbf{x}'^H]$ . Hence, the speech IFC vector  $\mathbf{r}_s$  and the speech PSD  $\phi_S$  in (8) can be computed as

$$\mathbf{r}_s = \mathbf{R}_x \mathbf{e}, \quad \phi_S = \mathbf{e}^T \mathbf{R}_x \mathbf{e} \quad (9)$$

with  $\mathbf{e} = [1, 0, \dots, 0]^T$  an  $M$ -dimensional selection vector. Considering the uncorrelated speech component  $\mathbf{x}'$  in (7) as an interference, we define the undesired signal vector  $\mathbf{u} = \mathbf{x}' + \mathbf{n}$  such that the *multi-frame signal model* is given by

$$\mathbf{y} = \boldsymbol{\gamma}_s S + \mathbf{u} \quad (10)$$

Using (10), the noisy speech correlation matrix in (6) can also be written as

$$\mathbf{R}_y = \phi_S \boldsymbol{\gamma}_s \boldsymbol{\gamma}_s^H + \mathbf{R}_u, \quad (11)$$

with the undesired correlation matrix  $\mathbf{R}_u = \mathbf{R}_{x'} + \mathbf{R}_n$ . Similarly to (8) and (9), the normalized noisy speech IFC vector  $\boldsymbol{\gamma}_y$  and normalized noise IFC vector  $\boldsymbol{\gamma}_n$  are defined as

$$\boldsymbol{\gamma}_y = \frac{\mathbf{r}_y}{\phi_Y} = \frac{\mathbf{R}_y \mathbf{e}}{\mathbf{e}^T \mathbf{R}_y \mathbf{e}}, \quad \boldsymbol{\gamma}_n = \frac{\mathbf{r}_n}{\phi_N} = \frac{\mathbf{R}_n \mathbf{e}}{\mathbf{e}^T \mathbf{R}_n \mathbf{e}}. \quad (12)$$

Using (6) and (12), it can be easily shown that

$$\phi_Y \boldsymbol{\gamma}_y = \phi_S \boldsymbol{\gamma}_s + \phi_N \boldsymbol{\gamma}_n. \quad (13)$$

## Speech-Distortion Weighted Filters

In this section, a SDW-WG is derived using the single-frame signal model and a C-SDW-IFWF and R-SDW-IFWF are derived using the multi-frame signal model. The filters incorporate a trade-off between noise reduction and speech distortion.

### SDW-WG

A cost-function for the SDW-WG can be designed which aims to minimize the speech distortion power as well as the output noise power, where the importance of each term can be weighted with a trade-off parameter  $\mu \in [0, \infty]$ , i.e.,

$$\hat{G} = \underset{G}{\operatorname{argmin}} \left\{ \underbrace{E[|GS - S|^2]}_{\text{Speech distortion power}} + \mu \underbrace{E[|GN|^2]}_{\text{Output noise power}} \right\}. \quad (14)$$

Solving this optimization problem leads to the real-valued SDW-WG

$$G_{\text{SDW-WG}} = \frac{\xi}{\mu + \xi} \quad (15)$$

with  $\xi = \frac{\phi_S}{\phi_N}$  the a-priori SNR.

### C-SDW-IFWF

Similarly to (14), the aim of the SDW-IFWF is to minimize the speech distortion power as well as the noise power, weighted with  $\mu$ , i.e.,

$$\hat{\mathbf{w}} = \underset{\mathbf{w}}{\operatorname{argmin}} \left\{ \underbrace{E[|\mathbf{w}^H \boldsymbol{\gamma}_s - S|^2]}_{\text{Speech distortion power}} + \mu \underbrace{E[|\mathbf{w}^H \mathbf{u}|^2]}_{\text{Output noise power}} \right\}. \quad (16)$$

Solving this optimization problem leads to the C-SDW-IFWF [1]

$$\mathbf{w}_{\text{SDW-IFWF}} = \frac{\mathbf{R}_y^{-1} \boldsymbol{\gamma}_s \phi_S}{\mu + (1 - \mu) \boldsymbol{\gamma}_s^H \mathbf{R}_y^{-1} \boldsymbol{\gamma}_s \phi_S}. \quad (17)$$

In [4], it was reported that this filter can be very sensitive to estimation errors for  $\mu > 0$ . Since it is well known that decomposing a multi-frame Wiener Filter into a multi-frame minimum-power distortionless-response (MFMPDR) filter and a postfilter leads to more robust results [5], we suggest to decompose the C-SDW-IFWF into an MFMPDR filter [1] and a postfilter

$$\mathbf{w}_{\text{SDW-IFWF}} = \underbrace{\frac{\mathbf{R}_y^{-1} \boldsymbol{\gamma}_s}{\boldsymbol{\gamma}_s^H \mathbf{R}_y^{-1} \boldsymbol{\gamma}_s}}_{\mathbf{w}_{\text{MFMPDR}}} \underbrace{\frac{\phi_S}{\mu \phi_U^{\text{out}} + \phi_S}}_{G_{\text{SDW-WG Postfilter}}} \quad (18)$$

where  $\phi_U^{\text{out}} = (\boldsymbol{\gamma}_s^H \mathbf{R}_u^{-1} \boldsymbol{\gamma}_s)^{-1}$  denotes the undesired signal PSD at the output of the MFMPDR filter.

### R-SDW-IFWF

As in [4], a real-valued, symmetric filter vector

$$\mathbf{W}[k, l] = \mathbf{D} \mathbf{w}[k, l] \quad (19)$$

can be derived, where  $\mathbf{D}$  is a discrete Fourier transform (DFT) matrix. Assuming that the noisy correlation matrix  $\mathbf{R}_y^{\text{circ}}$  is circulant structured, it can be defined as

$$\mathbf{R}_y^{\text{circ}}[k, l] = \frac{1}{2M} \mathbf{D}^H \boldsymbol{\Phi}_y[k, l] \mathbf{D}, \quad (20)$$

where  $\boldsymbol{\Phi}_y[k, l]$  is a diagonal matrix containing the neighbouring noisy PSD coefficients around the center frequency of a frequency bin  $k$ . The matrix  $\boldsymbol{\Phi}_y$  is obtained by windowing the PSDs  $\phi_Y[f, l]$  in a filterbank with a  $\frac{2M}{O}$  higher frequency-resolution, where  $O$  denotes the oversampling factor,

$$\boldsymbol{\Phi}_y[k, l](\tau, \tau) = \frac{1}{O} |H_F[\tau]|^2 \phi_Y \left[ \frac{2Mk}{O} + \tau, l \right], \quad \tau = -M + 1, -M + 2, \dots, M, \quad (21)$$

with  $H_F$  the  $F$ -point DFT of the zero-padded analysis window  $h_K$  and  $\boldsymbol{\Phi}_y[k, l](\tau, \tau)$  denotes the  $\tau$ -th diagonal element of the diagonal matrix  $\boldsymbol{\Phi}_y[k, l]$ . Similar approximations can be made for the correlation matrices  $\mathbf{R}_s^{\text{circ}}$

and  $\mathbf{R}_n^{circ}$  of speech and noise. Using (19) and (20) in (16), a R-SDW-IFWF can be derived

$$\mathbf{W}_{\text{SDW-IFWF}} = \frac{\Phi_{\mathbf{y}}^{-1} \Phi_{\mathbf{s}} \mathbf{1}}{\mu + (1 - \mu) \frac{\mathbf{1}^T \Phi_{\mathbf{s}} \Phi_{\mathbf{y}}^{-1} \Phi_{\mathbf{s}} \mathbf{1}}{\mathbf{1}^T \Phi_{\mathbf{s}} \mathbf{1}}} \quad (22)$$

This filter can be rewritten as a gain in the higher frequency resolution filterbank with  $F = \frac{2MK}{O}$  frequency bins by applying an overlap procedure

$$G[f, l] = \sum_{\nu = -\frac{O}{2} + 1}^{\frac{O}{2}} H_K \left[ f' + \frac{F}{K} \nu \right] \mathbf{W} \left[ \frac{K}{F} (f - f') + \nu, l \right] \left( f' + \frac{F}{K} \nu \right), \quad (23)$$

where  $H_K$  is the DFT of the analysis window  $h_K$  and

$$f' = \text{mod} \left( f + \frac{F}{K} - 1, \frac{F}{K} \right) - \frac{F}{K} + 1, \quad (24)$$

with  $\text{mod}()$  the modulo operator.

## Parameter Estimation

In this section, we present several estimators for the required parameters of the SDW-WG, C-SDW-IFWF, and R-SDW-IFWF.

### Real-Valued Filters

For the SDW-WG, an estimate of  $\xi$  is required, which is estimated using the decision-directed approach (DDA) in [6] with  $\phi_N$  estimated as in [7] in the high frequency resolution filterbank  $F$ .

For the R-SDW-IFWF, estimates of the speech and the noisy speech PSDs are required. The PSDs are estimated using periodograms in the high frequency resolution filterbank  $F$ . The noisy speech periodogram is given by

$$P_Y = |Y|^2. \quad (25)$$

The noisy PSD matrix  $\Phi_{\mathbf{y}}$  is estimated by replacing  $\phi_Y$  with  $P_Y$  in (21). The speech and noise periodograms are estimated by applying a Wiener gain (WG)  $G_{\text{WG}}$  (which is obtained by setting  $\mu = 1$  in (15)) to  $P_Y$ , i.e.,

$$\hat{P}_S = G_{\text{WG}} P_Y, \quad \hat{P}_N = (1 - G_{\text{WG}}) P_Y, \quad (26)$$

and the speech and noise PSD matrices  $\Phi_{\mathbf{s}}$  and  $\Phi_{\mathbf{n}}$  can be estimated similarly to  $\Phi_{\mathbf{y}}$ , by replacing  $\phi_Y$  with  $\hat{P}_S$  or  $\hat{P}_N$  in (21), respectively.

### Complex-valued filters

For the C-SDW-IFWF, estimates of  $\mathbf{R}_x$ ,  $\gamma_s$ ,  $\phi_S$ , and  $\mathbf{R}_u$  are required. The noisy speech correlation matrix  $\mathbf{R}_y$  can be estimated using first-order recursive smoothing as

$$\hat{\mathbf{R}}_y[k, l] = \lambda \hat{\mathbf{R}}_y[k, l - 1] + (1 - \lambda) \mathbf{y}[k, l] \mathbf{y}^H[k, l] \quad (27)$$

with  $\lambda$  a forgetting factor. The normalized speech IFC vector  $\gamma_s$  can be estimated as

$$\hat{\gamma}_s = \frac{\hat{\phi}_S + \hat{\phi}_N}{\hat{\phi}_S} \hat{\gamma}_y - \frac{\hat{\phi}_N}{\hat{\phi}_S} \frac{\hat{\mathbf{r}}_n}{\hat{\mathbf{r}}_n(1)} \quad (28)$$

where  $\gamma_y$  is estimated similarly to (12), using (27). In [5], we proposed to estimate the noise IFC vector  $\mathbf{r}_n$  from the  $F$  filterbank using the Wiener-Khinchin theorem similarly to [4]. The theorem states that the correlation of a wide-sense stationary process is given by the inverse DFT (IDFT) of the PSD. Hence, the noise IFC vector  $\mathbf{r}_n$  can be estimated by applying the IDFT to the noise periodograms in  $\hat{\Phi}_{\mathbf{n}}$ , i.e.,

$$\hat{\mathbf{r}}_n[k, l](m) = \frac{1}{2M} \sum_{\tau = -M+1}^M \hat{\Phi}_{\mathbf{n}}[k, l](\tau, \tau) e^{-j2\pi\tau m/2M}, \quad m = 0, 1, \dots, M - 1. \quad (29)$$

The speech PSD  $\phi_S$  is estimated by applying a WG to the noisy speech, i.e.  $\hat{\phi}_S = G_{\text{WG}} \hat{\phi}_Y$ , with  $\xi$  estimated using the DDA and  $\phi_N$  estimated using [7]. To estimate the output undesired PSD  $\phi_U^{\text{out}}$ , the undesired correlation matrix  $\mathbf{R}_u$  is estimated as

$$\hat{\mathbf{R}}_u = \hat{\mathbf{R}}_y - \hat{\phi}_S \hat{\gamma}_s \hat{\gamma}_s^H. \quad (30)$$

Due to estimation errors,  $\hat{\mathbf{R}}_u$  may not be positive semi-definite, thus, we set negative eigenvalues of  $\hat{\mathbf{R}}_u$  to zero.

## Experimental Results

In this section, we begin with describing the algorithmic implementation details and then we compare the performance of the presented SDW-WG and SDW-IFWFs in dependence of the trade-off parameter  $\mu$ .

### Implementation and Performance Measures

The performance compared to the noisy speech signal is evaluated in terms of the perceptual evaluation of speech quality (PESQ) [8] improvement and the segmental measures for speech distortion (sSD) and noise reduction (sNR) [9] as well as SNR improvement ( $\Delta$ sSNR)[2], using the clean speech signal as the reference signal. We used audio material from [10] sampled at 16 kHz. We evaluated the average performance over 105 s of speech material under five different noise conditions (babble, white Gaussian noise (WGN), traffic, modulated WGN, cross-road) at 0 dB and 10 dB input SNRs.

To achieve a high speech correlation, we use an STFT with a frame length of  $K = 64$  samples (4 ms) and a frame shift of 16 samples (1 ms) in the low frequency-resolution STFT filterbank. As analysis and synthesis window  $h_K$  we use a Hann window. The number of the consecutive time frames is  $M = 8$ , resulting in 11 ms of analysis data in the low frequency-resolution filterbank. In the high frequency-resolution STFT filterbank, we use a four-times higher frequency-resolution, i.e., a frame length of  $F = 256$  samples (16 ms), a frame shift of 16 samples (1 ms), and apply an asymmetric analysis window similarly to [4]. However,  $h_K$  is used as the synthesis window to maintain low synthesis delay (3 ms). In both filterbanks, the weighting parameter for the DDA [6] is set to 0.97. To reduce the amount of musical noise, the Wiener gain is limited to -17 dB. The forgetting factor in (27) is experimentally set to  $\lambda = 0.9$ , resulting in

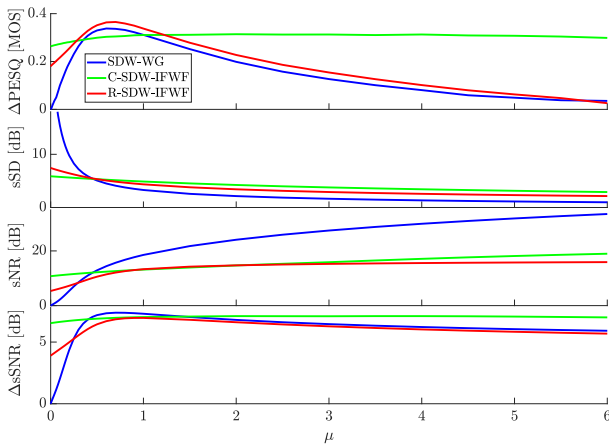


Figure 1: Averaged results at 0 dB SNR.

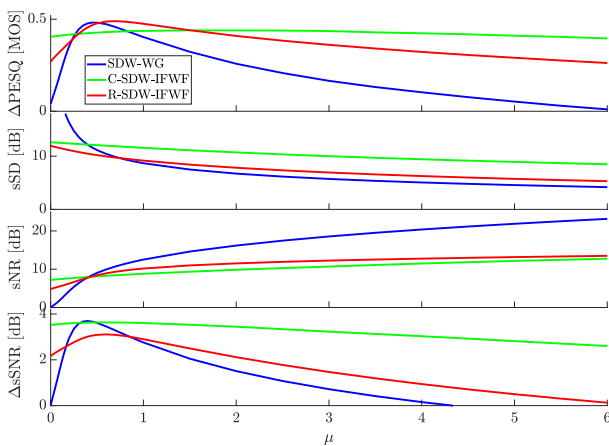


Figure 2: Averaged results at 10 dB SNR.

a smoothing window of 10 ms. Before computing  $\hat{\mathbf{R}}_y^{-1}$  in (18), regularization based on diagonal loading is performed with a regularization parameter of 0.04 as in [2].

### Comparison of SDW-IFWFs with SDW-WG

In Figs. 1, 2, the average PESQ, sSD, sNR, and  $\Delta$ sNR results at 0 dB and 10 dB SNR are depicted for the SDW-WG, C-SDW-IFWF, and R-SDW-IFWF. The R-SDW-IFWF leads to the highest PESQ improvement with  $\mu = 0.7$ , followed by the SDW-WG with  $\mu = 0.6$  at 0 dB and  $\mu = 0.45$  at 10 dB. The SDW-WG leads to the highest  $\Delta$ sNR scores with  $\mu = 0.7$  and  $\mu = 0.4$  at 0 dB and 10 dB, respectively. The SDW-WG leads to the highest NR scores for increasing  $\mu$ , however, simultaneously also the lowest SD scores. The C-SDW-IFWF outperforms all filters for all measures except for SD at  $\mu = 0$ . Only the SDW-WG achieves higher SD scores at  $\mu = 0$  since it applies no filtering, leaving the original signal unchanged and therefore the speech undistorted.

## CONCLUSION

In this paper, we evaluated the influence of the trade-off parameter in real- and complex-valued speech-distortion weighted filters, using a single- and multi-frame signal model, which balance noise reduction and speech distortion. We compared the performance for different speech and noise signals and signal-to-noise ratios, using prac-

tically feasible estimators for the required quantities. We showed that the R-SDW-IFWF achieves the highest speech quality improvement. Although the SDW-WG applies more noise reduction than multi-frame approaches, the C-SDW-IFWF, introduces less speech distortion.

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